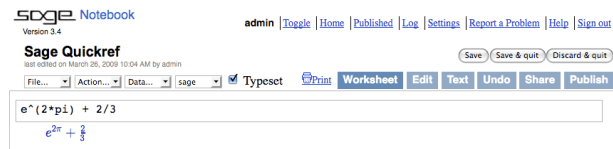


Sage Quick Reference

William Stein (based on work of P. Jipsen) (mod. by nu)
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Notebook Notebook



セルの評価: `<shift-enter>`

セルを評価し新しいセルを作る: `<alt-enter>`

セルの分割: `<control-; >`

セルの結合: `<control-backspace>`

数式セルの挿入: セルの間の青い線をクリック

Text/HTML セルの挿入: セルの間の青い線を shift-click

セルの削除: 内容を削除したあとで backspace

Evaluate cell: `<shift-enter>`

Evaluate cell creating new cell: `<alt-enter>`

Split cell: `<control-; >`

Join cells: `<control-backspace>`

Insert math cell: click blue line between cells

Insert text/HTML cell: shift-click blue line between cells

Delete cell: delete content then backspace

コマンドライン Command line

`com<tab>` で *command* を補完

`*bar*?` で “bar” を含むコマンド名をリストアップ

`command?<tab>` でドキュメントを表示

`command??<tab>` でソースコードを表示

`a.<tab>` でオブジェクト a のメソッドを表示 (`dir(a)` も)

`a._<tab>` で a の hidden methods を表示

`search_doc("string or regexp")` ドキュメントの全文検索

`search_src("string or regexp")` ソースコードの検索

`_` は直前の出力

`com<tab>` complete *command*

`*bar*?` list command names containing “bar”

`command?<tab>` shows documentation

`command??<tab>` shows source code

`a.<tab>` shows methods for object a (more: `dir(a)`)

`a._<tab>` shows hidden methods for object a

`search_doc("string or regexp")` fulltext search of docs

`search_src("string or regexp")` search source code

`_` is previous output

数 Numbers

整数: $\mathbb{Z} = \mathbb{ZZ}$ 例 `-2 -1 0 1 10^100`

有理数: $\mathbb{Q} = \mathbb{QQ}$ 例 `1/2 1/1000 314/100 -2/1`

実数: $\mathbb{R} \approx \mathbb{RR}$ 例 `.5 0.001 3.14 1.23e10000`

複素数: $\mathbb{C} \approx \mathbb{CC}$ 例 `CC(1,1) CC(2.5,-3)`

倍精度 (Double): `RDF` and `CDF` 例 `CDF(2.1,3)`

Mod n : $\mathbb{Z}/n\mathbb{Z} = \mathbb{Zmod}$ 例 `Mod(2,3) Zmod(3)(2)`

有限体: $\mathbb{F}_q = \mathbb{GF}$ 例 `GF(3)(2) GF(9,"a").0`

多項式: $R[x,y]$ 例 `S.<x,y>=QQ[] x+2*y^3`

巾級数: $R[[t]]$ 例 `S.<t>=QQ[] 1/2+2*t+0(t^2)`

p 進整数: $\mathbb{Z}_p \approx \mathbb{Zp}$, $\mathbb{Q}_p \approx \mathbb{Qp}$ 例 `2+3*5+0(5^2)`

代数閉包: $\overline{\mathbb{Q}} = \mathbb{QQbar}$ 例 `QQbar(2^(1/5))`

区間演算: `RIF` 例 `RIF((1,1.00001))`

数体: `R.<x>=QQ[]`; `K.<a>=NumberField(x^3+x+1)`

Integers: $\mathbb{Z} = \mathbb{ZZ}$ e.g. `-2 -1 0 1 10^100`

Rationals: $\mathbb{Q} = \mathbb{QQ}$ e.g. `1/2 1/1000 314/100 -2/1`

Reals: $\mathbb{R} \approx \mathbb{RR}$ e.g. `.5 0.001 3.14 1.23e10000`

Complex: $\mathbb{C} \approx \mathbb{CC}$ e.g. `CC(1,1) CC(2.5,-3)`

Double precision: `RDF` and `CDF` e.g. `CDF(2.1,3)`

Mod n : $\mathbb{Z}/n\mathbb{Z} = \mathbb{Zmod}$ e.g. `Mod(2,3) Zmod(3)(2)`

Finite fields: $\mathbb{F}_q = \mathbb{GF}$ e.g. `GF(3)(2) GF(9,"a").0`

Polynomials: $R[x,y]$ e.g. `S.<x,y>=QQ[] x+2*y^3`

Series: $R[[t]]$ e.g. `S.<t>=QQ[] 1/2+2*t+0(t^2)`

p -adic numbers: $\mathbb{Z}_p \approx \mathbb{Zp}$, $\mathbb{Q}_p \approx \mathbb{Qp}$ e.g. `2+3*5+0(5^2)`

Algebraic closure: $\overline{\mathbb{Q}} = \mathbb{QQbar}$ e.g. `QQbar(2^(1/5))`

Interval arithmetic: `RIF` e.g. `RIF((1,1.00001))`

Number field: `R.<x>=QQ[]`; `K.<a>=NumberField(x^3+x+1)`

四則演算など Arithmetic

$ab = a*b$ $\frac{a}{b} = a/b$ $a^b = a^b$ $\sqrt{x} = \text{sqrt}(x)$

$\sqrt[n]{x} = x^(1/n)$ $|x| = \text{abs}(x)$ $\log_b(x) = \text{log}(x,b)$

和: $\sum_{i=k}^n f(i) = \text{sum}(f(i) \text{ for } i \text{ in } (k..n))$

積: $\prod_{i=k}^n f(i) = \text{prod}(f(i) \text{ for } i \text{ in } (k..n))$

$ab = a*b$ $\frac{a}{b} = a/b$ $a^b = a^b$ $\sqrt{x} = \text{sqrt}(x)$

$\sqrt[n]{x} = x^(1/n)$ $|x| = \text{abs}(x)$ $\log_b(x) = \text{log}(x,b)$

Sums: $\sum_{i=k}^n f(i) = \text{sum}(f(i) \text{ for } i \text{ in } (k..n))$

Products: $\prod_{i=k}^n f(i) = \text{prod}(f(i) \text{ for } i \text{ in } (k..n))$

定数と関数 Constants and functions

定数: $\pi = \text{pi}$ $e = \text{e}$ $i = \text{i}$ $\infty = \text{oo}$

$\phi = \text{golden_ratio}$ $\gamma = \text{euler_gamma}$

近似値: `pi.n(digits=18) = 3.14159265358979324`

関数: `sin cos tan sec csc cot sinh cosh tanh sech csch coth log ln exp ...`

Python の関数: `def f(x): return x^2`

Constants: $\pi = \text{pi}$ $e = \text{e}$ $i = \text{i}$ $\infty = \text{oo}$

$\phi = \text{golden_ratio}$ $\gamma = \text{euler_gamma}$

Approximate: `pi.n(digits=18) = 3.14159265358979324`

Functions: `sin cos tan sec csc cot sinh cosh tanh sech csch coth log ln exp ...`

Python function: `def f(x): return x^2`

インタラクティブな操作 Interactive functions

関数の前に `@interact` を置く (変数で controls が決まる)

`@interact`

```
def f(n=[0..4], s=(1..5), c=Color("red")):
    var("x")
    show(plot(sin(n+x^s),-pi,pi,color=c))
```

Put `@interact` before function (vars determine controls)

`@interact`

```
def f(n=[0..4], s=(1..5), c=Color("red")):
    var("x")
    show(plot(sin(n+x^s),-pi,pi,color=c))
```

シンボリックな数式 Symbolic expressions

新しい不定元 (symbolic variables) を定義: `var("t u v y z")`

シンボリックな関数 (Symbolic function):

例 $f(x) = x^2$ `f(x)=x^2`

関係式: `f==g f<=g f>=g f<g f>g`

$f = g$ を解く: `solve(f(x)==g(x), x)`

`solve([f(x,y)==0, g(x,y)==0], x,y)`

`factor(...)` `expand(...)` `(...).simplify...`

$x \in [a,b]$ s.t. $f(x) \approx 0$ を見付ける: `find_root(f(x), a, b)`

Define new symbolic variables: `var("t u v y z")`

Symbolic function: e.g. $f(x) = x^2$ `f(x)=x^2`

Relations: `f==g f<=g f>=g f<g f>g`

Solve $f = g$: `solve(f(x)==g(x), x)`

`solve([f(x,y)==0, g(x,y)==0], x,y)`

`factor(...)` `expand(...)` `(...).simplify...`

`find_root(f(x), a, b)` `find x \in [a,b] s.t. f(x) \approx 0`

微分積分 Calculus

$\lim_{x \rightarrow a} f(x) = \text{limit}(f(x), x=a)$

$\frac{d}{dx}(f(x)) = \text{diff}(f(x), x)$

$\frac{\partial}{\partial x}(f(x,y)) = \text{diff}(f(x,y), x)$

`diff = differentiate = derivative`

$\int f(x)dx = \text{integral}(f(x), x)$

$\int_a^b f(x)dx = \text{integral}(f(x), x, a, b)$

$\int_a^b f(x)dx \approx \text{numerical_integral}(f(x), a, b)$

a に関する次数 n の Taylor 多項式: `taylor(f(x), x, a, n)`

$\lim_{x \rightarrow a} f(x) = \text{limit}(f(x), x=a)$

$\frac{d}{dx}(f(x)) = \text{diff}(f(x), x)$

$\frac{\partial}{\partial x}(f(x,y)) = \text{diff}(f(x,y), x)$

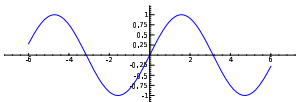
`diff = differentiate = derivative`

$\int f(x)dx = \text{integral}(f(x), x)$

$\int_a^b f(x)dx = \text{integral}(f(x), x, a, b)$

$\int_a^b f(x)dx \approx \text{numerical_integral}(f(x), a, b)$
Taylor polynomial, deg n about a : $\text{taylor}(f(x), x, a, n)$

二次元グラフィックス 2D graphics



`line([(x1,y1), ..., (xn,yn)], options)`
`polygon([(x1,y1), ..., (xn,yn)], options)`
`circle((x,y), r, options)`

`text("txt", (x,y), options)`

`options` は `plot.options` にあるものを使用,
例 `thickness=pixel`, `rgbcolor=(r,g,b)`, `hue=h`
ただし $0 \leq r, b, g, h \leq 1$

`show(graphic, options)`

サイズの調整には `figsize=[w,h]` を使う

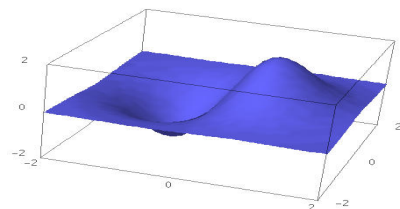
縦横比を調整するには `aspect_ratio=number` を使う

`plot(f(x), (x, xmin, xmax), options)`
`parametric_plot((f(t), g(t)), (t, tmin, tmax), options)`
`polar_plot(f(t), (t, tmin, tmax), options)`
結合: `circle((1,1), 1)+line([(0,0), (2,2)])`

`animate(list of graphics, options).show(delay=20)`

```
line([(x1,y1), ..., (xn,yn)], options)
polygon([(x1,y1), ..., (xn,yn)], options)
circle((x,y), r, options)
text("txt", (x,y), options)
options as in plot.options,
  e.g. thickness=pixel, rgbcolor=(r,g,b), hue=h
  where 0 ≤ r, b, g, h ≤ 1
show(graphic, options)
  use figsize=[w,h] to adjust size
  use aspect_ratio=number to adjust aspect ratio
plot(f(x), (x, xmin, xmax), options)
parametric_plot((f(t), g(t)), (t, tmin, tmax), options)
polar_plot(f(t), (t, tmin, tmax), options)
combine: circle((1,1), 1)+line([(0,0), (2,2)])
animate(list of graphics, options).show(delay=20)
```

三次元グラフィックス 3D graphics



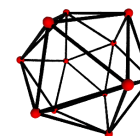
`line3d([(x1,y1,z1), ..., (xn,yn,zn)], options)`
`sphere((x,y,z), r, options)`

```
text3d("txt", (x,y,z), options)
tetrahedron((x,y,z), size, options)
cube((x,y,z), size, options)
octahedron((x,y,z), size, options)
dodecahedron((x,y,z), size, options)
icosahedron((x,y,z), size, options)
plot3d(f(x,y), (x,xb,xe), (y,yb,ye), options)
parametric_plot3d((f,g,h), (t,tb,te), options)
parametric_plot3d((f(u,v), g(u,v), h(u,v)),
  (u,ub,ue), (v,vb,ve), options)
options: aspect_ratio=[1,1,1], color="red",
  opacity=0.5, figsize=6, viewer="tachyon"
line3d([(x1,y1,z1), ..., (xn,yn,zn)], options)
sphere((x,y,z), r, options)
text3d("txt", (x,y,z), options)
tetrahedron((x,y,z), size, options)
cube((x,y,z), size, options)
octahedron((x,y,z), size, options)
dodecahedron((x,y,z), size, options)
icosahedron((x,y,z), size, options)
plot3d(f(x,y), (x,xb,xe), (y,yb,ye), options)
parametric_plot3d((f,g,h), (t,tb,te), options)
parametric_plot3d((f(u,v), g(u,v), h(u,v)),
  (u,ub,ue), (v,vb,ve), options)
options: aspect_ratio=[1,1,1], color="red",
  opacity=0.5, figsize=6, viewer="tachyon"
```

離散数学 Discrete math

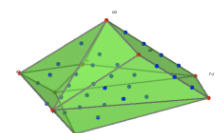
```
[x] = floor(x)   [x] = ceil(x)
n を k で割った余り = n%k   k|n iff n%k==0
n! = factorial(n)   (x choose m) = binomial(x,m)
phi(n) = euler_phi(n)
文字列 (String): 例 s = "Hello" = "He"+"llo"
  s[0]="H"   s[-1]="o"   s[1:3]="el"   s[3:]="lo"
リスト (List): 例 [1, "Hello", x] = []+[1, "Hello"]+[x]
タプル (Tuple): 例 (1, "Hello", x) (immutable)
集合 (Set): 例 {1, 2, 1, a} = Set([1, 2, 1, "a"]) (= {1, 2, a})
集合の内包的記法 ≈ リストの内包表記, 例
{f(x)|x ∈ X, x > 0} = Set([f(x) for x in X if x > 0])
[x] = floor(x)   [x] = ceil(x)
Remainder of n divided by k = n%k   k|n iff n%k==0
n! = factorial(n)   (x choose m) = binomial(x,m)
phi(n) = euler_phi(n)
Strings: e.g. s = "Hello" = "He"+"llo"
  s[0]="H"   s[-1]="o"   s[1:3]="el"   s[3:]="lo"
Lists: e.g. [1, "Hello", x] = []+[1, "Hello"]+[x]
Tuples: e.g. (1, "Hello", x) (immutable)
Sets: e.g. {1, 2, 1, a} = Set([1, 2, 1, "a"]) (= {1, 2, a})
List comprehension ≈ set builder notation, e.g.
{f(x)|x ∈ X, x > 0}
```

グラフ理論 Graph theory



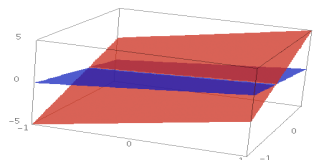
グラフ: `G = Graph({0:[1,2,3], 2:[4]})`
有向グラフ: `DiGraph(dictionary)`
グラフの族: `graphs.<tab>`
不変量: `G.chromatic_polynomial()`, `G.is_planar()`
パス: `G.shortest_path()`
可視化: `G.plot()`, `G.plot3d()`
自己同型: `G.automorphism_group()`,
`G1.is_isomorphic(G2)`, `G1.is_subgraph(G2)`
Graph: `G = Graph({0:[1,2,3], 2:[4]})`
Directed Graph: `DiGraph(dictionary)`
Graph families: `graphs.<tab>`
Invariants: `G.chromatic_polynomial()`, `G.is_planar()`
Paths: `G.shortest_path()`
Visualize: `G.plot()`, `G.plot3d()`
Automorphisms: `G.automorphism_group()`,
`G1.is_isomorphic(G2)`, `G1.is_subgraph(G2)`

組合せ論 Combinatorics



整数列: `sloane_find(list)`, `sloane.<tab>`
分割: `P=Partitions(n)` `P.count()`
組合せ (部分リスト): `C=Combinations(list)` `C.list()`
直積: `CartesianProduct(P,C)`
ヤング盤 (Tableau): `Tableau([[1,2,3], [4,5]])`
ワード: `W=Words("abc"); W("aabca")`
半順序集合 (poset): `Poset([[1,2], [4], [3], [4], []])`
ルート系: `RootSystem(["A", 3])`
クリスタル: `CrystalOfTableaux(["A", 3], shape=[3,2])`
格子多面体: `A=random_matrix(ZZ, 3, 6, x=7)`
`L=LatticePolytope(A)` `L.npoints()` `L.plot3d()`
Integer sequences: `sloane_find(list)`, `sloane.<tab>`
Partitions: `P=Partitions(n)` `P.count()`
Combinations: `C=Combinations(list)` `C.list()`
Cartesian product: `CartesianProduct(P,C)`
Tableau: `Tableau([[1,2,3], [4,5]])`
Words: `W=Words("abc"); W("aabca")`
Posets: `Poset([[1,2], [4], [3], [4], []])`
Root systems: `RootSystem(["A", 3])`

Crystals: CrystalOfTableaux(["A",3], shape=[3,2])
Lattice Polytopes: A=random_matrix(ZZ,3,6,x=7)
L=LatticePolytope(A) L.npoints() L.plot3d()



行列代数 Matrix algebra

$\begin{pmatrix} 1 \\ 2 \end{pmatrix} = \text{vector}([1,2])$
 $\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \text{matrix}(\text{QQ}, [[1,2],[3,4]], \text{sparse}=\text{False})$
 $\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{pmatrix} = \text{matrix}(\text{QQ}, 2, 3, [1,2,3, 4,5,6])$
 $\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = \text{det}(\text{matrix}(\text{QQ}, [[1,2],[3,4]]))$
 $Av = A*v \quad A^{-1} = A^{-1} \quad A^t = A.\text{transpose}()$
 $Ax = v$ を解く: $A \setminus v$ or $A.\text{solve_right}(v)$
 $xA = v$ を解く: $A.\text{solve_left}(v)$
被約行階段行列: $A.\text{echelon_form}()$
階数と退化: $A.\text{rank}()$ $A.\text{nullity}()$
Hessenberg 型: $A.\text{hessenberg_form}()$
特性多項式: $A.\text{charpoly}()$
固有値: $A.\text{eigenvalues}()$
固有ベクトル: $A.\text{eigenvectors_right}()$ (also left)
Gram-Schmidt: $A.\text{gram_schmidt}()$
可視化: $A.\text{plot}()$
LLL reduction: $\text{matrix}(\text{ZZ}, \dots).\text{LLL}()$
Hermite 形式: $\text{matrix}(\text{ZZ}, \dots).\text{hermite_form}()$
 $\begin{pmatrix} 1 \\ 2 \end{pmatrix} = \text{vector}([1,2])$
 $\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \text{matrix}(\text{QQ}, [[1,2],[3,4]], \text{sparse}=\text{False})$
 $\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{pmatrix} = \text{matrix}(\text{QQ}, 2, 3, [1,2,3, 4,5,6])$
 $\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = \text{det}(\text{matrix}(\text{QQ}, [[1,2],[3,4]]))$
 $Av = A*v \quad A^{-1} = A^{-1} \quad A^t = A.\text{transpose}()$
Solve $Ax = v$: $A \setminus v$ or $A.\text{solve_right}(v)$
Solve $xA = v$: $A.\text{solve_left}(v)$
Reduced row echelon form: $A.\text{echelon_form}()$
Rank and nullity: $A.\text{rank}()$ $A.\text{nullity}()$
Hessenberg form: $A.\text{hessenberg_form}()$
Characteristic polynomial: $A.\text{charpoly}()$
Eigenvalues: $A.\text{eigenvalues}()$
Eigenvectors: $A.\text{eigenvectors_right}()$ (also left)
Gram-Schmidt: $A.\text{gram_schmidt}()$
Visualize: $A.\text{plot}()$
LLL reduction: $\text{matrix}(\text{ZZ}, \dots).\text{LLL}()$
Hermite form: $\text{matrix}(\text{ZZ}, \dots).\text{hermite_form}()$

線形代数 Linear algebra

ベクトル空間 $K^n = K^n$ 例 $\text{QQ}^3 \text{RR}^2 \text{CC}^4$

部分空間: $\text{span}(\text{vectors}, \text{field})$

例 $\text{span}([[1,2,3], [2,3,5]], \text{QQ})$

Kernel: $A.\text{right_kernel}()$ (left_ も)

和と共通部分: $V + W$ と $V.\text{intersection}(W)$

基底: $V.\text{basis}()$

基底行列: $V.\text{basis_matrix}()$

行列を部分空間への制限: $A.\text{restrict}(V)$

基底を使ったベクトルの表示: $V.\text{coordinates}(\text{vector})$

Vector space $K^n = K^n$ e.g. $\text{QQ}^3 \text{RR}^2 \text{CC}^4$

Subspace: $\text{span}(\text{vectors}, \text{field})$

E.g., $\text{span}([[1,2,3], [2,3,5]], \text{QQ})$

Kernel: $A.\text{right_kernel}()$ (also left)

Sum and intersection: $V + W$ and $V.\text{intersection}(W)$

Basis: $V.\text{basis}()$

Basis matrix: $V.\text{basis_matrix}()$

Restrict matrix to subspace: $A.\text{restrict}(V)$

Vector in terms of basis: $V.\text{coordinates}(\text{vector})$

数値計算 Numerical mathematics

パッケージ: `import numpy, scipy, cvxopt`

最小化: `var("x y z")`

`minimize(x^2+x*y^3+(1-z)^2-1, [1,1,1])`

Packages: `import numpy, scipy, cvxopt`

Minimization: `var("x y z")`

`minimize(x^2+x*y^3+(1-z)^2-1, [1,1,1])`

整数論 Number theory

素数: `prime_range(n,m)`, `is_prime`, `next_prime`

素因数分解: `factor(n)`, `qsieve(n)`, `ecm.factor(n)`

Kronecker symbol: $\left(\frac{a}{b}\right) = \text{kronecker_symbol}(a,b)$

連分数: `continued_fraction(x)`

Bernoulli 数: `bernoulli(n)`, `bernoulli_mod_p(p)`

楕円曲線: `EllipticCurve([a1, a2, a3, a4, a6])`

Dirichlet characters: `DirichletGroup(N)`

Modular forms: `ModularForms(level, weight)`

Modular symbols: `ModularSymbols(level, weight, sign)`

Brandt modules: `BrandtModule(level, weight)`

Modular abelian varieties: `J0(N)`, `J1(N)`

Primes: `prime_range(n,m)`, `is_prime`, `next_prime`

Factor: `factor(n)`, `qsieve(n)`, `ecm.factor(n)`

Kronecker symbol: $\left(\frac{a}{b}\right) = \text{kronecker_symbol}(a,b)$

Continued fractions: `continued_fraction(x)`

Bernoulli numbers: `bernoulli(n)`, `bernoulli_mod_p(p)`

Elliptic curves: `EllipticCurve([a1, a2, a3, a4, a6])`

Dirichlet characters: `DirichletGroup(N)`

Modular forms: `ModularForms(level, weight)`

Modular symbols: `ModularSymbols(level, weight, sign)`

Brandt modules: `BrandtModule(level, weight)`

Modular abelian varieties: `J0(N)`, `J1(N)`

群論 Group theory

$G = \text{PermutationGroup}([(1,2,3), (4,5)], [(3,4)])$

$\text{SymmetricGroup}(n)$, $\text{AlternatingGroup}(n)$

アーベル群: $\text{AbelianGroup}([3,15])$

行列群: GL , SL , Sp , SU , GU , SO , GO

関数: $G.\text{syllow_subgroup}(p)$, $G.\text{character_table}()$,

$G.\text{normal_subgroups}()$, $G.\text{cayley_graph}()$

$G = \text{PermutationGroup}([(1,2,3), (4,5)], [(3,4)])$

$\text{SymmetricGroup}(n)$, $\text{AlternatingGroup}(n)$

Abelian groups: $\text{AbelianGroup}([3,15])$

Matrix groups: GL , SL , Sp , SU , GU , SO , GO

Functions: $G.\text{syllow_subgroup}(p)$, $G.\text{character_table}()$,

$G.\text{normal_subgroups}()$, $G.\text{cayley_graph}()$

非可換環 Noncommutative rings

四元数: $Q.<i,j,k> = \text{QuaternionAlgebra}(a,b)$

自由代数: $R.<a,b,c> = \text{FreeAlgebra}(\text{QQ}, 3)$

Quaternions: $Q.<i,j,k> = \text{QuaternionAlgebra}(a,b)$

Free algebra: $R.<a,b,c> = \text{FreeAlgebra}(\text{QQ}, 3)$

Python のモジュール Python modules

`import module_name`

`module_name.<tab>` and `help(module_name)`

`import module_name`

`module_name.<tab>` and `help(module_name)`

解析とデバッグ Profiling and debugging

`time command`: timing information の表示

`timeit("command")`: accurately time command

`t = cputime()`; `cputime(t)`: 経過した CPU time

`t = walltime()`; `walltime(t)`: 経過した wall time

`%pdb`: interactive debugger を開始 (command line only)

`%prun command`: profile command (command line only)

`time command`: show timing information

`timeit("command")`: accurately time command

`t = cputime()`; `cputime(t)`: elapsed CPU time

`t = walltime()`; `walltime(t)`: elapsed wall time

`%pdb`: turn on interactive debugger (command line only)

`%prun command`: profile command (command line only)